

GUIDE 98-1

Uncertainty of measurement -

Part 1:

Introduction to the expression of uncertainty in measurement

First edition 2009

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ISO/IEC Foreword

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ISO/IEC Guide 98-1 was prepared by Working Group 1 of the Joint Committee for Guides in Metrology (as JCGM 104:2009), and was adopted by the national bodies of ISO and IEC.

ISO/IEC Guide 98 consists of the following parts, under the general title Uncertainty of measurement:

- Part 1: Introduction to the expression of uncertainty in measurement
- Part 3: Guide to the expression of uncertainty in measurement (GUM:1995)

The following parts are planned:

- Part 2: Concepts and basic principles
- Part 4: Role of measurement uncertainty in conformity assessment
- Part 5: Applications of the least-squares method

ISO/IEC Guide 98-3 has one supplement.

— Supplement 1: Propagation of distributions using a Monte Carlo method

The following supplements to ISO/IEC Guide 98-3 are planned:

- Supplement 2: Models with any number of output quantities
- Supplement 3: Modelling

Given that ISO/IEC Guide 98-1:2009 is identical in content to JCGM 104:2009, the decimal symbol is a point on the line in the English version.

Annex ZZ has been appended to provide a list of corresponding ISO/IEC Guides and JCGM guidance documents for which equivalents are not given in the text.

104 2009

Evaluation of measurement data — An introduction to the "Guide to the expression of uncertainty in measurement" and related documents

Évaluation des données de mesure – Une introduction au "Guide pour l'expression de l'incertitude de mesure" et aux documents qui le concernent

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U	ontents	Page
Fo	preword	. v
Introduction		. vi
1	Scope	. 1
2	Normative references	. 2
3	What is measurement uncertainty?	. 2
4	Concepts and basic principles	. 4
5	Stages of uncertainty evaluation	. 8
6	The formulation stage: developing a measurement model	. 9
7	The calculation (propagation and summarizing) stage of uncertainty evaluation7.1General7.2The GUM uncertainty framework7.3Analytic methods7.4Monte Carlo method7.5Measurement models with any number of output quantities	. 10 . 11 . 12 . 13
8	Measurement uncertainty in conformity assessment	. 14
9	Applications of the least-squares method	. 15
Annexes		
Α	Acronyms and initialisms	. 16
Bi	Bibliography	
\mathbf{A}	Alphabetical index	

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In 1997 a Joint Committee for Guides in Metrology (JCGM), chaired by the Director of the BIPM, was created by the seven international organizations that had originally in 1993 prepared the 'Guide to the expression of uncertainty in measurement' (GUM) and the 'International vocabulary of metrology – basic and general concepts and associated terms' (VIM). The JCGM assumed responsibility for these two documents from the ISO Technical Advisory Group 4 (TAG4).

The Joint Committee is formed by the BIPM with the International Electrotechnical Commission (IEC), the International Federation of Clinical Chemistry and Laboratory Medicine (IFCC), the International Laboratory Accreditation Cooperation (ILAC), the International Organization for Standardization (ISO), the International Union of Pure and Applied Chemistry (IUPAC), the International Union of Pure and Applied Physics (IUPAP), and the International Organization of Legal Metrology (OIML).

JCGM has two Working Groups. Working Group 1, 'Expression of uncertainty in measurement', has the task to promote the use of the GUM and to prepare Supplements and other documents for its broad application. Working Group 2, 'Working Group on International vocabulary of basic and general terms in metrology (VIM)', has the task to revise and promote the use of the VIM. For further information on the activity of the JCGM, see www.bipm.org.

The present document has been prepared by Working Group 1 of the JCGM, and has benefited from detailed reviews undertaken by member organizations of the JCGM.

This document constitutes one part in a series of JCGM documents under the generic heading *Evaluation of* measurement data. The parts in the series are

- JCGM 100:2008. Evaluation of measurement data Guide to the expression of uncertainty in measurement (GUM) (see clause 2),
- JCGM 101:2008. Evaluation of measurement data Supplement 1 to the "Guide to the expression of uncertainty in measurement" Propagation of distributions using a Monte Carlo method (see clause 2),
- JCGM 102. Evaluation of measurement data Supplement 2 to the "Guide to the expression of uncertainty in measurement" – Models with any number of output quantities,
- JCGM 103. Evaluation of measurement data Supplement 3 to the "Guide to the expression of uncertainty in measurement" – Modelling,
- JCGM 104. Evaluation of measurement data An introduction to the "Guide to the expression of uncertainty in measurement" and related documents [this document],
- JCGM 105. Evaluation of measurement data Concepts and basic principles,
- JCGM 106. Evaluation of measurement data The role of measurement uncertainty in conformity assessment, and
- JCGM 107. Evaluation of measurement data Applications of the least-squares method.

Introduction

A statement of measurement uncertainty is indispensable in judging the fitness for purpose of a measured quantity value. At the greengrocery store the customer would be content if, when buying a kilogram of fruit, the scales gave a value within, say, 2 grams of the fruit's actual weight. However, the dimensions of components of the gyroscopes within the inertial navigation systems of commercial aircraft are checked by measurement to parts in a million for correct functioning.

Measurement uncertainty is a general concept associated with any measurement and can be used in professional decision processes as well as judging attributes in many domains, both theoretical and experimental. As the tolerances applied in industrial production become more demanding, the role of measurement uncertainty becomes more important when assessing conformity to these tolerances. Measurement uncertainty plays a central role in quality assessment and quality standards.

Measurement is present in almost every human activity, including but not limited to industrial, commercial, scientific, healthcare, safety and environmental. Measurement helps the decision process in all these activities. Measurement uncertainty enables users of a measured quantity value to make comparisons, in the context of conformity assessment, to obtain the probability of making an incorrect decision based on the measurement, and to manage the consequential risks.

This document serves as an introduction to measurement uncertainty, the GUM and the related documents indicated in the Foreword. A probabilistic basis for uncertainty evaluation is used. Annex <u>A</u> gives acronyms and initialisms used in this document.

In future editions of JCGM 200 (VIM) it is intended to make a clear distinction between the use of the term *error* as a quantity and as a quantity value. The same statement applies to the term *indication*. In the current document such a distinction is made. JCGM 200:2008 does not distinguish explicitly between these uses.